

## Senior Project

# A comparison of intraday solar power forecasting methods

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# Introduction

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## Why intraday forecasting is essential ?

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The **volatile nature** of solar resource has posed the difficulties in grid management as solar penetration rate grows continuously.

An **intraday forecasting** task becomes important for

1. Power plant operation
2. Grid balancing
3. Real-time unit dispatching

# Objective

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- To study the relevant variables of intraday solar irradiance forecasting.
- To compare forecasting models including LR, MARS, ANN, SVR, RF in the aspects of
  - Forecasting performance
  - Computational complexity

# 02

## Methodology

Notation:

- $I$ : solar irradiance [ $\text{W}/\text{m}^2$ ]
- $P$ : solar Power [ $\text{kW}$ ]
- $\theta$ : solar zenith angle
- $x(t)$ :  $x$  at execution time
- $x(t + k)$ :  $x$  in 30k-min ahead
- $x^{(d-1)}(t)$ : value of  $x$  in day  $d - 1$  at time  $t$
- $\hat{x}(t)$ : forecasted value of  $x$  at time  $t$

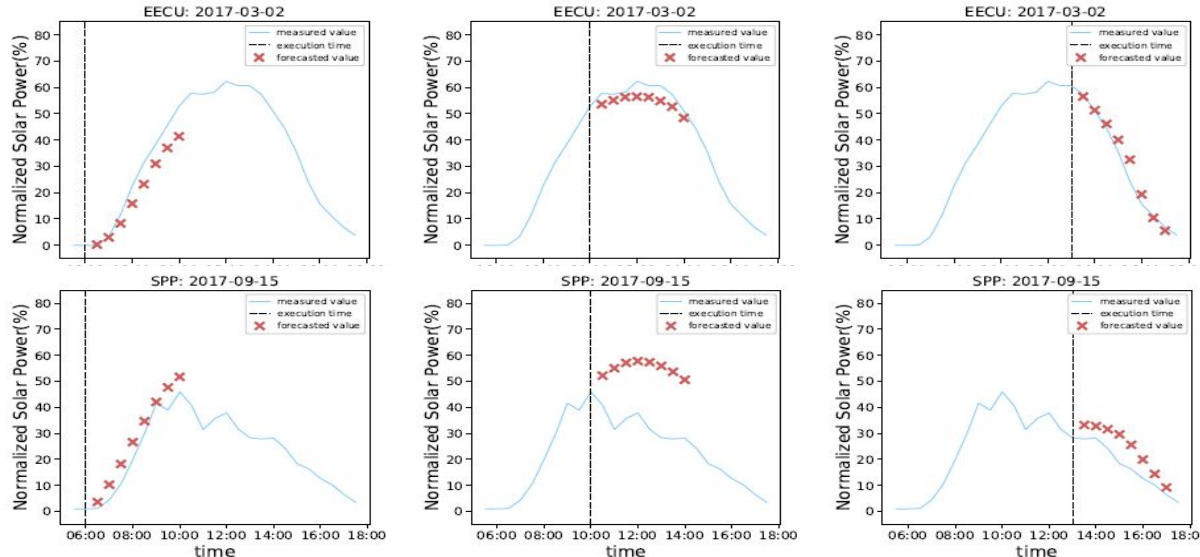
# Forecasting Configuration

Goal: predict solar power with the horizon of 4 hours every 30 minutes

$$\hat{P}(t+1), \hat{P}(t+2), \dots, \hat{P}(t+8)$$

Time of forecast values: 6:00 - 17:30: every 30 min

Execution time: 5:30 - 17:00



In **clear sky** days,  
the solar power prediction is quite  
**straightforward**.

In **general** days,  
the solar power prediction  
Is a **challenging problem** especially at  
**midday**.

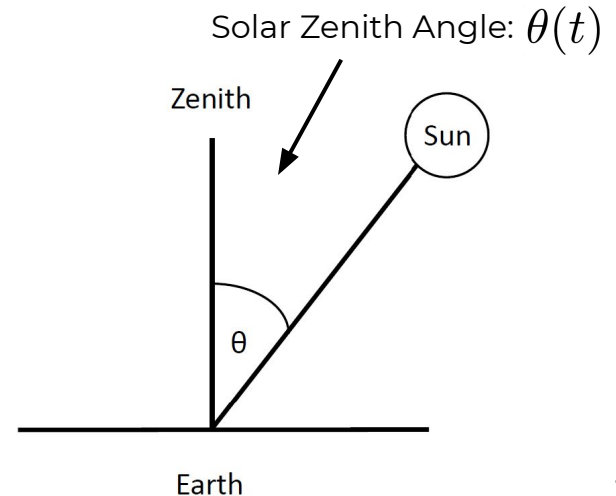
# Clear sky models

Clear sky models estimate the terrestrial solar radiation under a **cloudless sky** as a function of the solar elevation angle and various atmospheric conditions.

Berger-Duffie model [Vio97]:  $I_{\text{clr}}(t) = 956.27 \cos(\theta(t))$

ASHRAE model [PC07]:  $I_{\text{clr}}(t) = K e^{-B \sec(\theta(t))}$

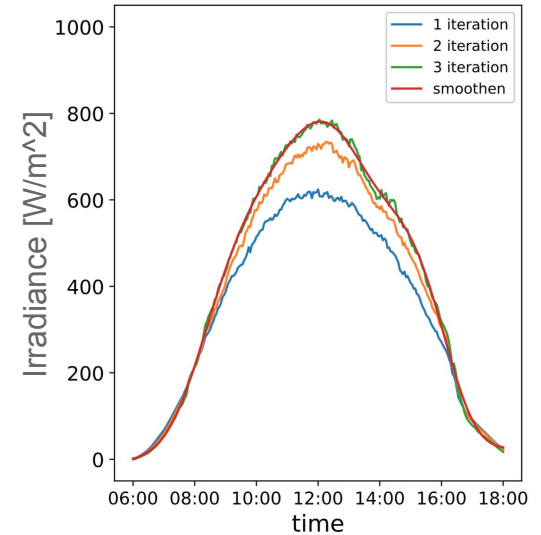
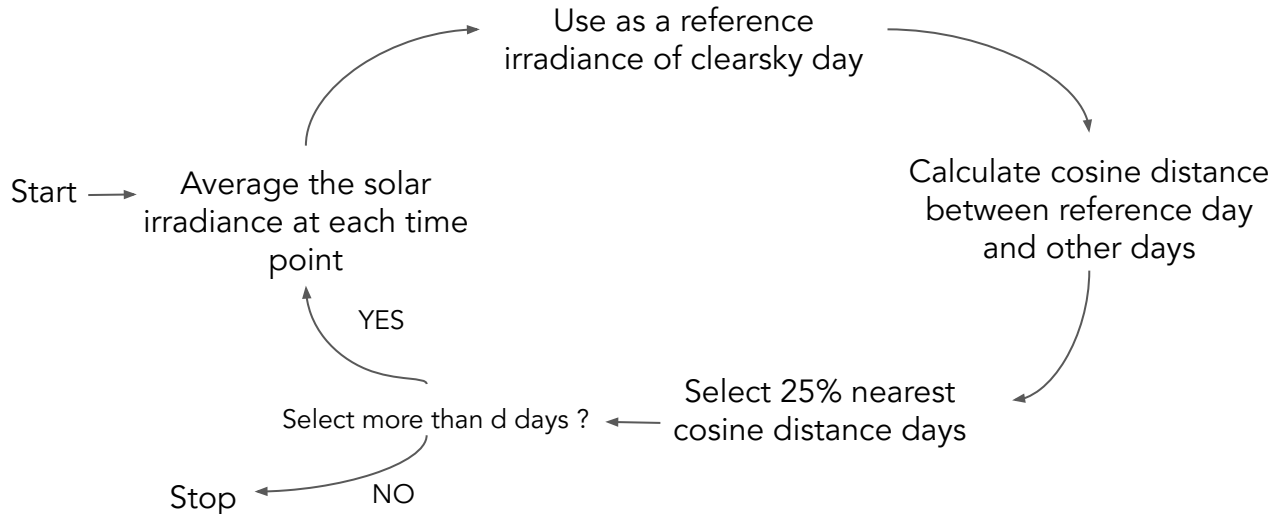
$K$ ,  $B$  are constant **estimated by measurement data**.



# Clear sky detection algorithm

Concept: we will find the reference clearsky day then select the days that are similar to this day as a clearsky day. [we use cosine distance to measure similarity]

- Finding reference clearsky day



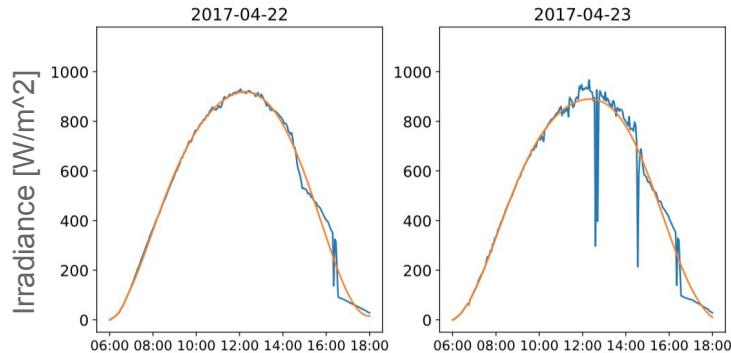
Example of reference clearsky days : EECU



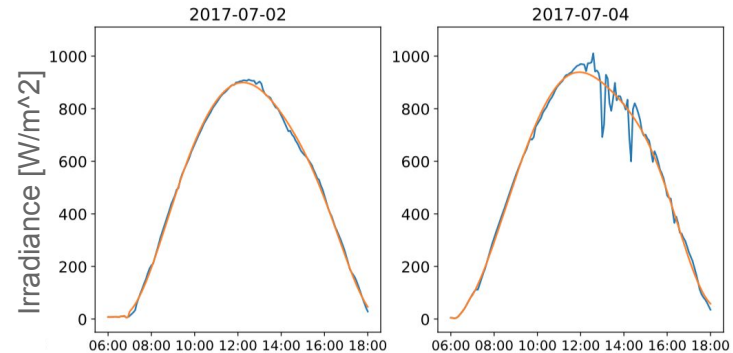
# Clear sky detection algorithm

Concept : we will find the reference clearsky day then select the days that are similar to this day as a clearsky day. [we use cosine distance to measure similarity]

- Select clearsky days: set cosine distance threshold for selecting clearsky day
- Smoothen the data: apply bi-directional butterworth low-pass filter



Example of selected clearsky days : EECU

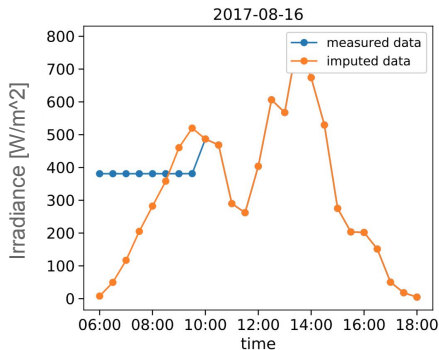


Example of selected clearsky days : SPP

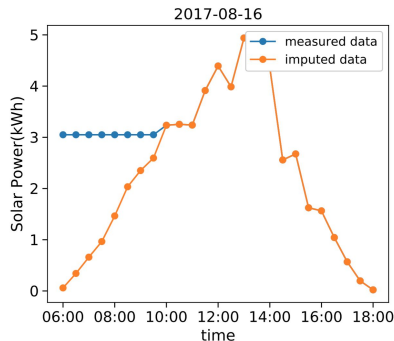
# Data preprocessing: data verification

We found **abnormal patterns** in some irradiance and power data

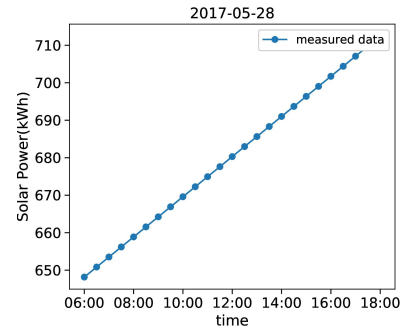
1. Data are held constant **more than 2 hrs** (but not entire day).
  - Replace with an ( $\pm 15$  days) average of solar irradiance at that time point
2. Data are held constant for **entire day** or have **unnatural pattern**.
  - Delete an information of that day



Example of constant irradiance : EECU



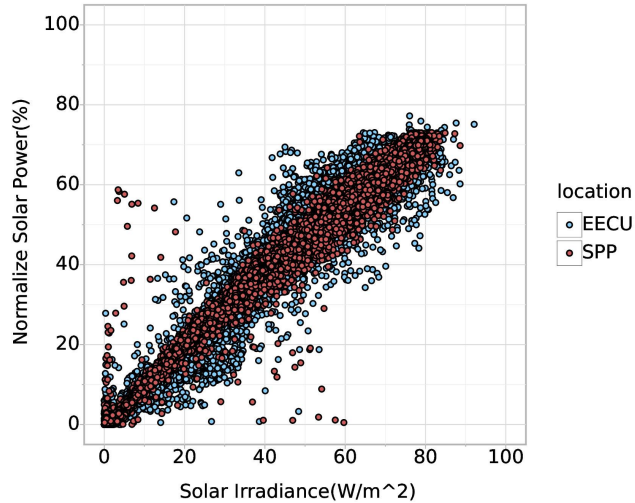
Example of constant power : EECU



Example of unnatural pattern in power : SPP

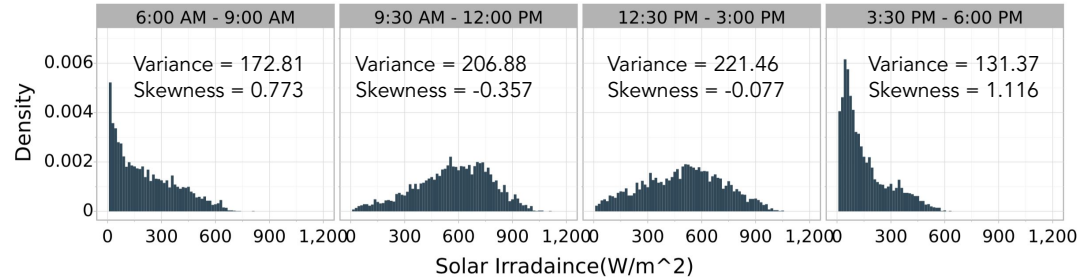
# Data pre-analysis

Relationship between Solar Irradiance and Normalized Solar Power

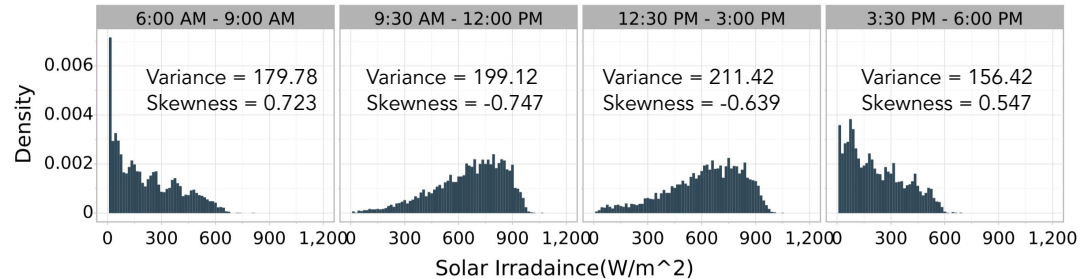


The Irradiance and power at SPP have stronger relationship than at EECU

distribution of Irradiance in each time of forecast: EECU



distribution of Irradiance in each time of forecast: SPP



The distribution can be separated into 3 groups: morning/midday/evening  
The SPP have lower variance/skewness than EECU

# Forecasting technique

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- Baseline models
  - Linear regression (LR)
  - Multivariate adaptive regression splines (MARS)
  - Artificial neural network (ANN)
- Proposed models
  - Support vector regression (SVR)
  - Random Forest (RF)

# Baseline model: Linear Regression & MARS

## MARS:

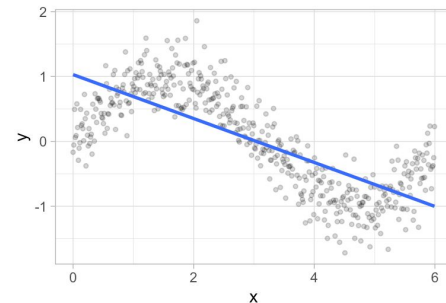
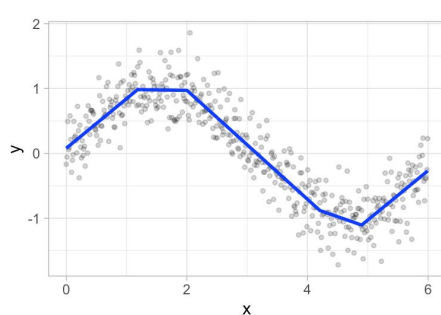
MARS capture the nonlinear relationships in the data by **assessing cutpoints** (knots) using expansions in **piecewise linear basis functions** [FHT01]

Target:

- $\hat{I}(t+1), \hat{I}(t+2), \dots, \hat{I}(t+8)$

Input:

- $I(t), I(t-1), \dots, I(t-7)$
- $I^{(d-1)}(t+k), k = 1, 2, \dots, 8$
- $I_{\text{clr}}(t+k), k = 1, 2, \dots, 8$



Example of MARS & Linear regression

# Baseline model: Artificial Neural Network (ANN)

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Artificial neural network model **proposed from SGRU** has the following architecture

1. Input layer: consist of
  - $I(t)$
  - $I_{\text{ema}}^{(d-1)}(t+k), k = 1, 2, \dots, 8$
  - $P(t)$
  - $T(t)$
2. Hidden layer: fully connected 5 hidden layers, each hidden layer consist of 128 neurons
3. Output layer:
  - $\hat{I}(t+1), \hat{I}(t+2), \dots, \hat{I}(t+8)$

# Proposed model: Random Forest & SVR


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## Random Forest (RF)

Random forest is an ensemble regressor that consists of many regression trees.[FHT01]

## Support Vector Regression

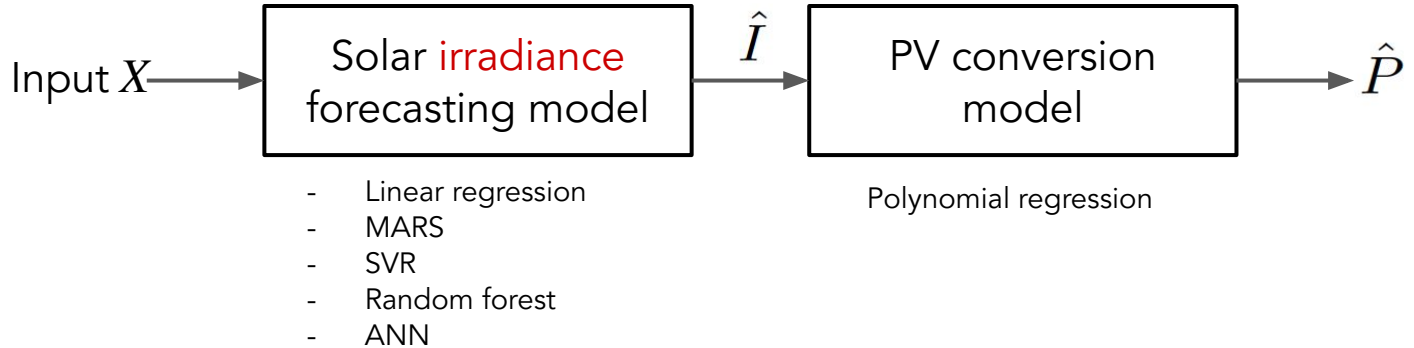
SVR is a regression technique based on the concepts of support vector. The idea is to find the function that minimize the  $\epsilon$ -loss function and at the same time, as flat as possible [SS04]



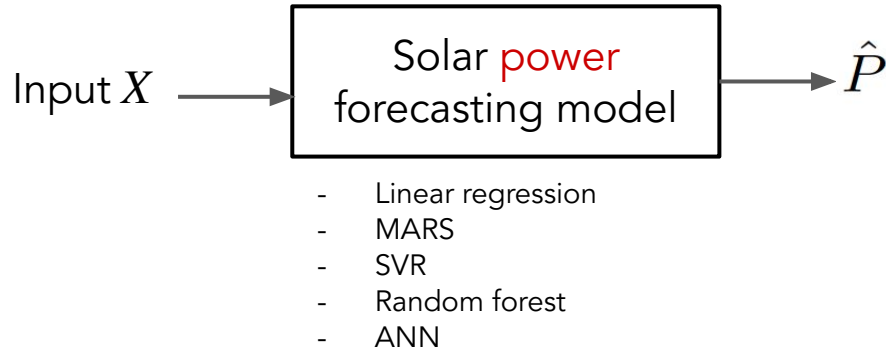
This 2 approaches are **split** and responsible for providing forecasting values at **morning, midday and evening**.

# Forecasting approaches

## Indirect approach

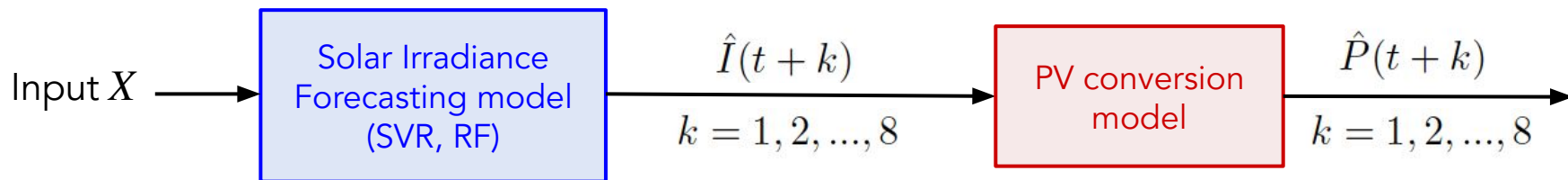


## Direct approach





## Indirect approach



### Morning model:

Input

- $I(t)$
- $I^{(d-1)}(t+k)$
- $\cos(\theta(t+k))$
- $I_{\text{clr}}(t+k)$

### Midday model:

Input

- $I(t), I(t-1), \dots, I(t-7)$
- $I_{\text{ema}}(t)$
- $I^{(d-1)}(t+k)$
- $\cos(\theta(t+k))$
- $I_{\text{clr}}(t+k)$

### Evening model:

Input

- $I(t)$
- $I^{(d-1)}(t+k)$
- $\cos(\theta(t+k))$
- $I_{\text{clr}}(t+k)$

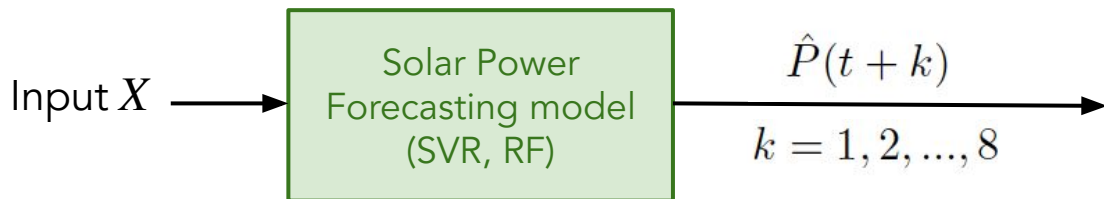
### Polynomial model:

$$P(I) = a_1 I + a_2 I^2 + a_3 I^3$$

When  $a_1, a_2, a_3$  are constant estimated by measurement data.

## Direct approach

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### Morning model:

Input

- $I(t)$
- $P^{(d-1)}(t+k)$
- $P(t)$
- $I_{\text{clr}}(t+k)$
- $\cos(\theta(t+k))$

### Midday model:

Input

- $I(t), I(t-1), \dots, I(t-7)$
- $P(t), P(t-1), \dots, P(t-7)$
- $P_{\text{ema}}(t)$
- $I_{\text{clr}}(t+k)$
- $P^{(d-1)}(t+k)$
- $\cos(\theta(t+k))$

### Evening model:

Input

- $I(t)$
- $P^{(d-1)}(t+k)$
- $P(t)$
- $I_{\text{clr}}(t+k)$
- $\cos(\theta(t+k))$

# 03

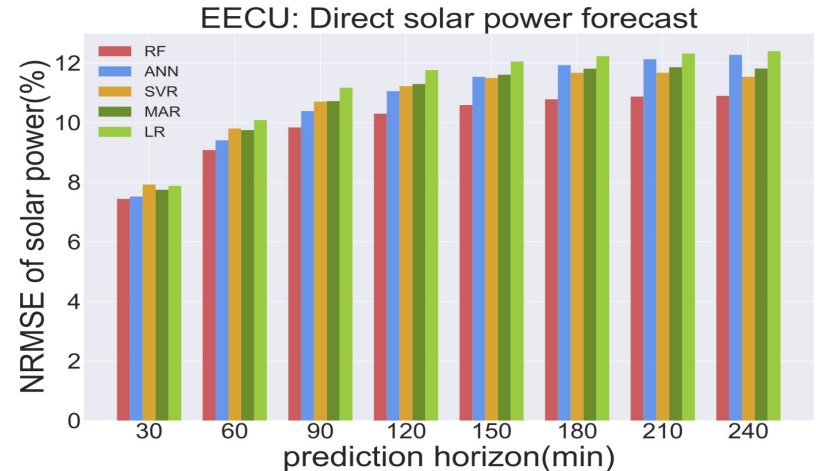
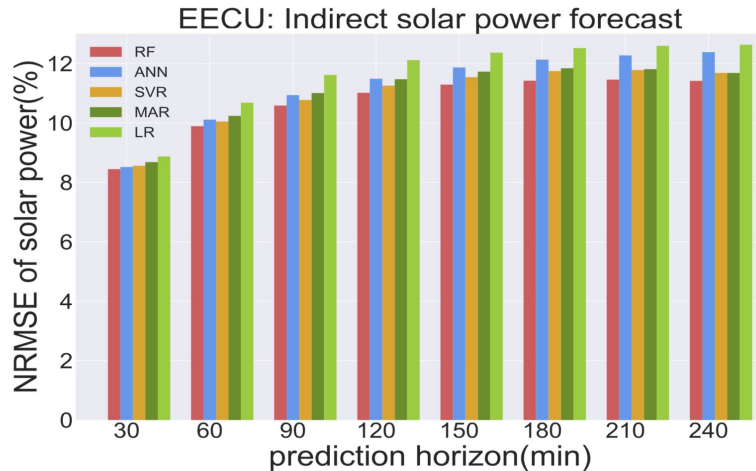
## Result & Discussion

Performance comparison between direct & indirect approach

- NRMSE versus prediction horizon at EECU/SPP  
Represent the forecast accuracy in each prediction horizon
- NRMSE versus time of forecasted values at EECU/SPP  
Represent the forecast accuracy in each time point
- NMBE versus time of forecasted values at EECU/SPP  
Show that the model overestimate/underestimate solar the power which may lead to over operating cost and lacking power in power distribution system respectively

# Performance comparison between direct & indirect approach

## - NRMSE versus prediction horizon at EECU

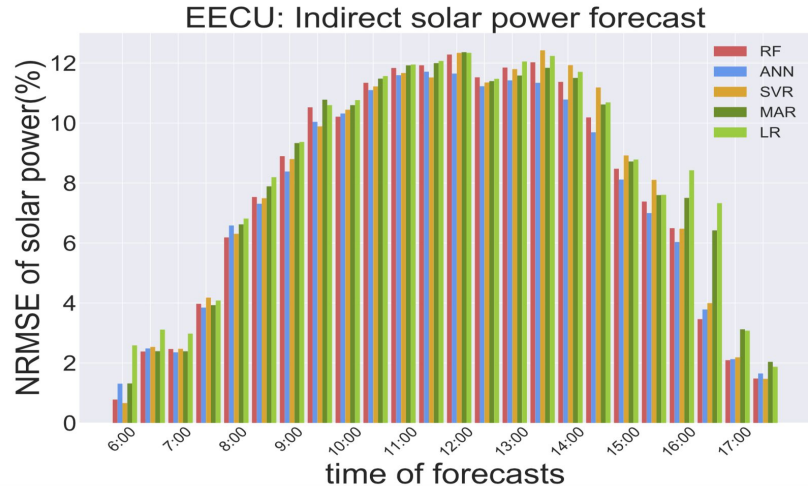
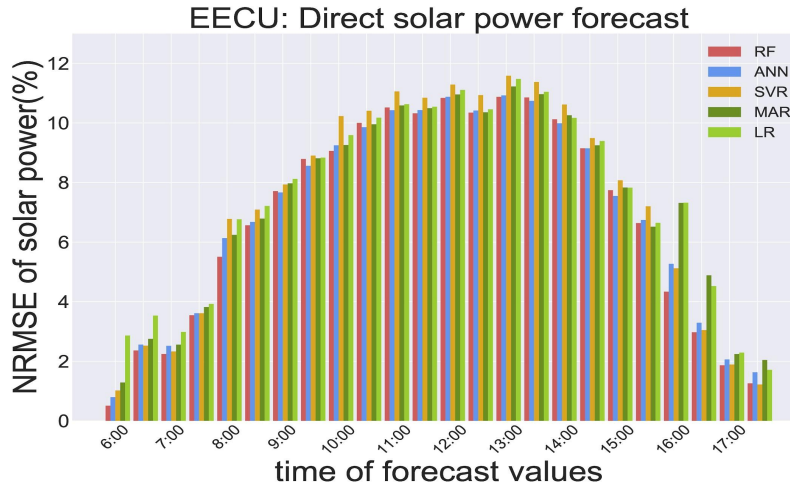


- Direct approach: random forest achieved the best performance. (7.44% in 30-min ahead)
- Linear regression which is the simplest model have the worst performance.
- The proposed models achieved the **better performance than the baseline and showed the competing result with the former literature.**

(1-hour ahead) Direct approach random forest : 9.08% , Direct approach SVR : 9.80%  
 [VKSB16] SARIMA : 8.12% , [BMP13] (SARIMA-SVR) 9.40%

# Performance comparison between direct & indirect approach

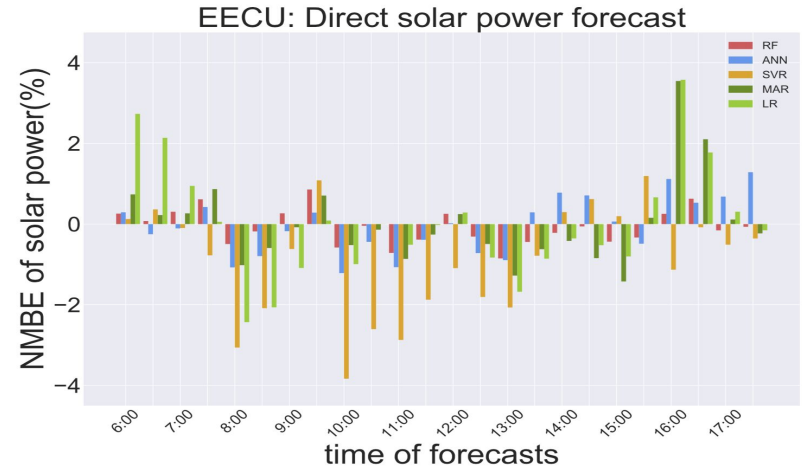
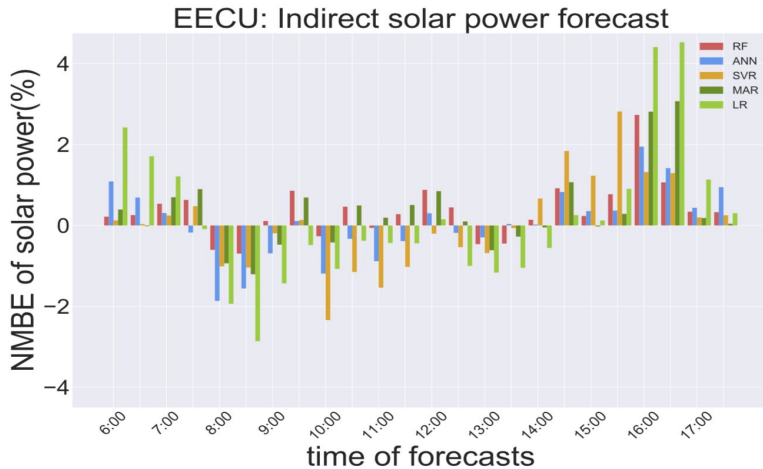
- NRMSE versus time of forecasted values at EECU



- NRMSE in the midday is usually higher than in the morning/evening
- The worst performance appear at 1:00-2:00 p.m. in both direct & indirect approach.
  - Direct approach RF: 10.12%
  - Direct approach SVR: 10.61%
- Linear regression and MARS reported high error at 4:00-5:00 p.m. due to rapid drop of solar irradiance

# Performance comparison between direct & indirect approach

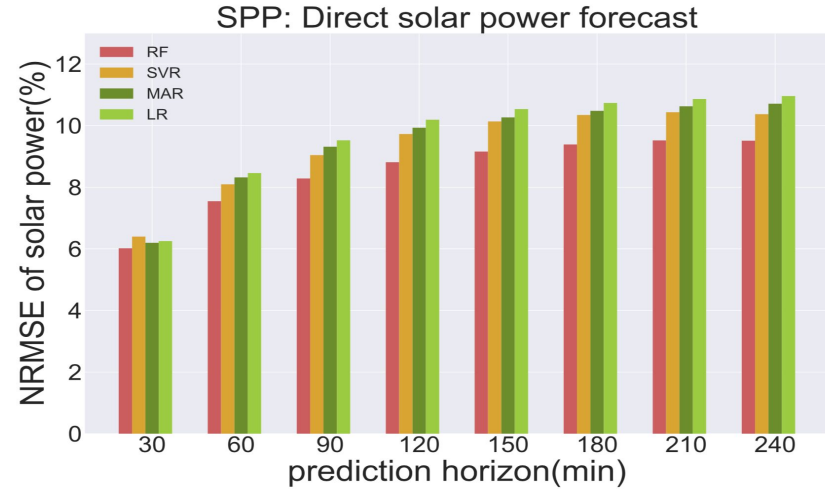
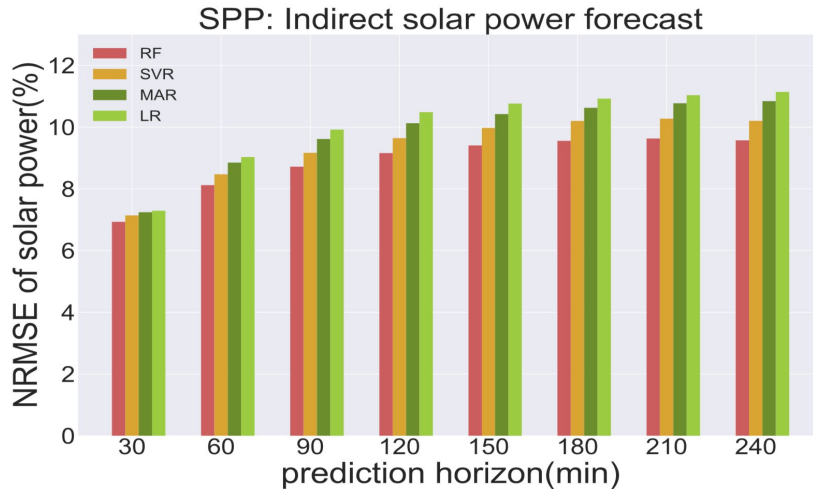
- NMBE versus time of forecasted at EECU



- Direct approach: random forest achieved the best performance.
- Direct approach: SVR is usually underestimate the solar power. This may lead to over operating cost.
- LR & MARS tend to overestimate the solar power at 4:00 - 4:30 p.m. This may lead to lacking power in power distribution system.

# Performance comparison between direct & indirect approach

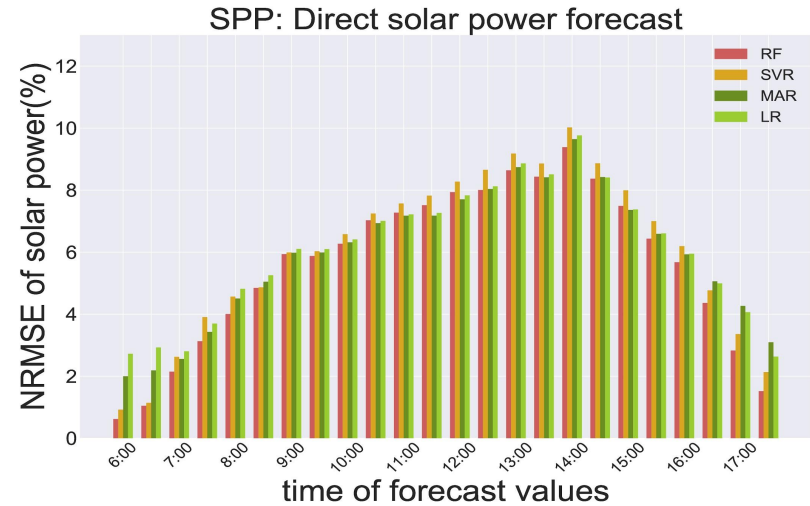
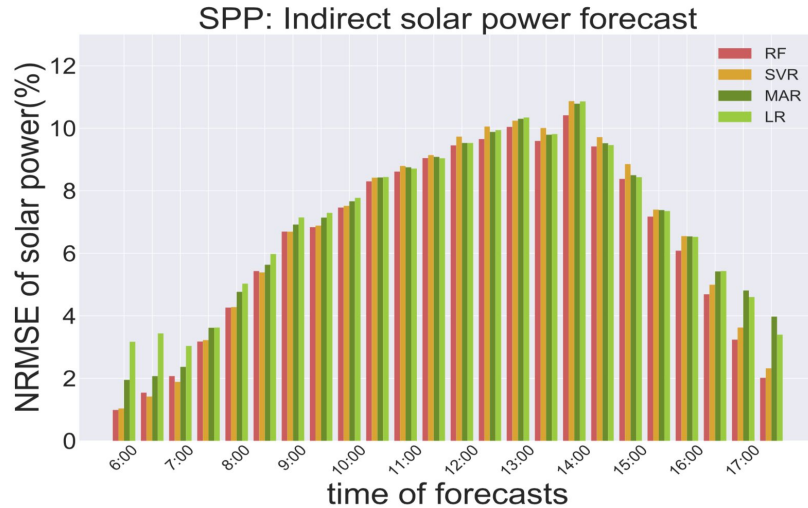
- NRMSE versus prediction horizon at SPP



- Direct approach random forest still achieved the best performance in every prediction horizon.  
30 min-ahead: 6.02%      240 min-ahead: 9.51%
- The result showed the **competing result with the former literature**.  
(1-hour ahead) Direct approach random forest : 7.55%      Direct approach SVR : 8.09%  
[VKSB16] SARIMA : 8.12%      [BMP13] (SARIMA-SVR) 9.40%

# Performance comparison between direct & indirect approach

- NRMSE versus time of forecasted values at SPP

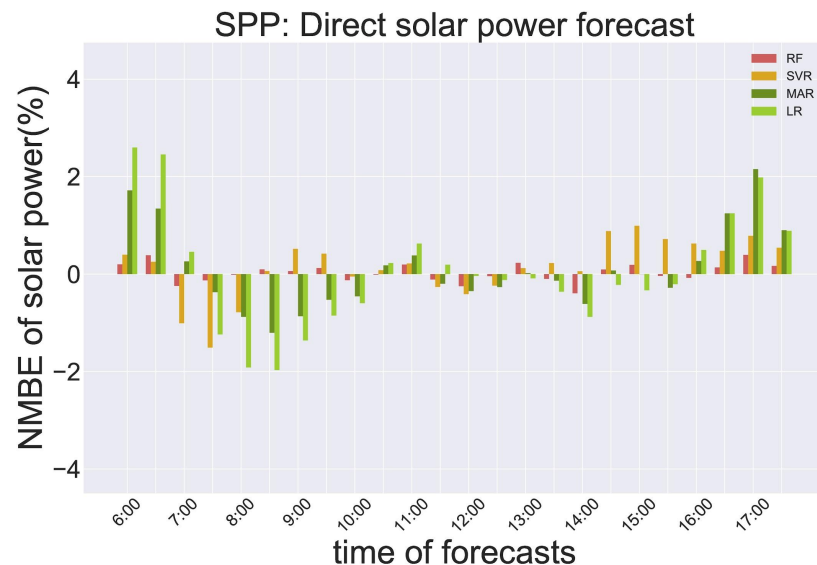
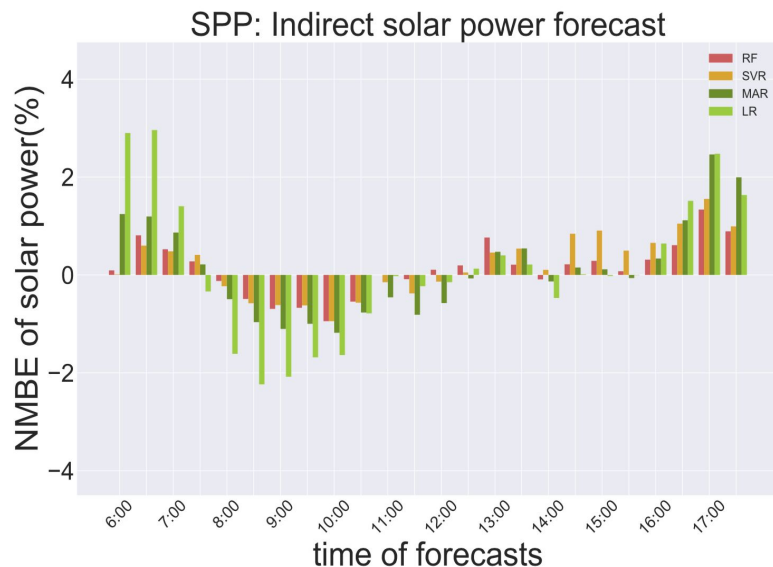


- NRMSE in the midday is usually higher than in the morning/evening
- The worst performance appear at 2.00 p.m. in both direct & indirect approach.
- The results showed the same pattern with EECU.



# Performance comparison between direct & indirect approach

- NMBE versus time of forecasted values at SPP



- In the evening, we usually overestimate the solar power
- Overall error at SPP is lower than at EECU in accordance with the result from data pre-analysis.

# Computational complexity

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Main complexities consist of 3 parts

1. Feature computation
  - Calculate feature, e.g. exponential moving average of solar irradiance
2. Model training
  - Fitting model, e.g. Least square (linear regression), Binary splitting (random forest)
  - The most computational complex part but, can be an **offline task**
3. Prediction
  - Calculate prediction values
  - **The most concerned part** in real-time prediction (especially for intraday forecast)

# Computational complexity

Hyper-parameter:

- $p$ : number of feature
- $M$ : number of basis (MARS)
- $S$ : number of support vector (SVR)
- $n_{\text{tree}}$ : number of tree in forest (RF)
- $d$ : tree depth (RF)
- $q$ : number of hidden layer (ANN)
- $t$ : number of neuron in outer layer (ANN)
- $r$ : number of neuron in inner layer (ANN)

Method	Prediction
Linear regression	$O(p)$
MARS	$O(Mp)$
SVR	$O(Sp)$
RF	$O(n_{\text{tree}}d)$
ANN	$O(pr + r(q - 1) + rt)$

Reference: [RSO14], [Fri93], [CM16], [Joh99]

# Computational complexity

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Complexity in prediction process (for hyper-parameter in this application):

LR < MARS < SVR < RF < ANN

But not significantly different in this application (in terms of computation time)



# Conclusion

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## Conclusion: Forecasting approaches

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- The result shows that **the direct** approach yielded better performance than **the indirect** approach because the error from irradiance prediction combining with the error from conversion model are greater than the error from direct power prediction.
- The forecast accuracy at **SPP** is better than **EECU** in every prediction horizon due to the different data characteristic. (e.g. variance, skewness)

## Conclusion: Comparing to the literature

- The best model in every prediction horizon in terms of forecast accuracy is achieved by the **direct approach: random forest model**

NRMSE (%)	30-min ahead	1-hour ahead	2-hour ahead
SPP	6.02	7.55	8.81
EECU	7.44	9.08	10.30

- Compare to the literature,
  - [VKSB16] (SARIMA) achieved 8.12% NRMSE for 1-hour ahead
  - [BMP13] (SARIMA-SVR) achieved 9.40% NRMSE for 1-hour ahead
  - [XCS12] (SVR) achieved 9.34% NRMSE for 2-hour ahead



Q&A

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Thank you



# Reference (1)

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- [Vio97] B. Viorel. Verification of some very simple clear and cloudy sky models to evaluate global solar irradiance. *Solar Energy*, 61(4):251–264, 1997.
- [PC07] A. Pansak and S. Chumnong. An assessment of the ashrae clear sky model for irradiance prediction in thailand. *Asian J. Energy Environ*, 8(02):523–532, 2007.
- [FHT01] J. Friedman, T. Hastie, and R. Tibshirani. *The elements of statistical learning*, volume 1. Springer series in statistics New York, 2001.
- [SS04] Smola, A.J., Schölkopf, B. A tutorial on support vector regression. *Statistics and Computing* volume 14. 199–222, 2004.

## Reference (2)

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- [RSO14] L. Roi, S. Shwartz, and S. Ohad. On the computational efficiency of training neural networks. In Z. Ghahramani, M. Welling, C. Cortes, N. D. Lawrence, and K. Q. Weinberger, editors, *Advances in Neural Information Processing Systems 27*, pages 855–863. Curran Associates, Inc., 2014.
- [Fri93] J. Friedman. Fast MARS. Technical report, Technical Report, 1993
- [XCS12] R. Xu, H. Chen, and X. Sun. Short-term photovoltaic power forecasting with weighted support vector machine. In *2012 IEEE International Conference on Automation and Logistics*, pages 248–253. IEEE, 2012.

## Reference (3)

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- [CM16] G. Callejas and A. Miguel. The effects of model and data complexity on predictions from species distributions models. *Ecological Modelling*, 326:4–12, 2016
- [Joh99] P. John. Fast training of support vector machines using sequential minimal optimization. *advances in kernel methods—support vector learning* (pp. 185–208). AJ, MIT Press, Cambridge, MA, 1999.
- [BMP13] M. Bouzerdoum, A. Mellit, and A.M. Pavan. A hybrid model (SARIMA–SVM) for short-term power forecasting of a small-scale grid-connected photovoltaic plant. *Solar Energy*, 98:226–235, 2013.

## Reference (4)

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- [VKSB16] S. Vagropoulos, G. Chouliaras and . Kardakos and, C. Simoglou, and A. Bakirtzis. Comparison of SARIMAX, SARIMA, modified SARIMA and ANN-based models for short-term PV generation forecasting. In 2016 IEEE International Energy Conference (ENERGYCON), pages 1–6. IEEE, 2016.